

## PROTEIN – LIGAND BINDING

(Precaution to be taken to avoid the occurrence of wrong result)

Manjunath.R

#16/1, 8th Main Road, Shivanagar, Rajajinagar, Bangalore560010, Karnataka, India

\*Corresponding Author Email: [manjunath5496@gmail.com](mailto:manjunath5496@gmail.com)

### ABSTRACT

The dissociation of a protein – ligand complex (PL) can be described by a simple equilibrium reaction  $PL \rightleftharpoons P + L$  the corresponding equilibrium relationship is defined  $K [PL] = [P] [L]$  ( $K =$  dissociation constant) In this equation  $[P] = [P]_T - [PL]$  and  $[L] = [L]_T - [PL]$  where  $[P]_T$  and  $[L]_T$  are the initial total concentrations of the protein and ligand, respectively. **Case1:** If we substitute  $[L]_T - [PL]$  for  $[L]$  and  $[P]_T - [PL]$  for  $[P]$ , then equilibrium relationship becomes  $K [PL] = ([L]_T - [PL]) ([P]_T - [PL])$  From this it follows that  $[PL] = [L]_T [P] / K + [P]$  **Case2:** If we substitute  $[L]_T - [PL]$  for  $[L]$ ,  $[P]_T - [PL]$  for  $[P]$  and  $[P]_T - [P]$  for  $[PL]$ , then equilibrium relationship becomes  $K ([P]_T - [P]) = ([L]_T - [PL]) ([P]_T - [PL])$  From this it follows that  $K - [L] = K F_{FP} - F_{BP} [L]$  (wrong result) **Conclusion:** Substitution for '[PL]' along with the substitutions for '[L]' and '[P]' should be avoided in order to prevent the occurrence of wrong result.

### KEYWORDS

Protein –ligand binding, protein - ligand complex, equilibrium reaction, dissociation constant.

### CASE 1

Using the equilibrium relationship

$K [PL] = [L] [P]$  and substituting,

$[L]_T - [PL]$  for  $[L]$

$[P]_T - [PL]$  for  $[P]$

Gives:

$$K [PL] = \{[L]_T - [PL]\} \{[P]_T - [PL]\}$$

$$= [L]_T [P]_T - [PL] [L]_T - [PL] [P]_T + [PL]^2$$

Dividing throughout by  $[PL]$  gives:

$$K = \{[L]_T [P]_T / [PL]\} - [L]_T - [P]_T + [PL]$$

But

$$[P]_T = [PL] + [P]$$

And, therefore,

$$K = \{[L]_T [P]_T / [PL]\} - [L]_T - [P]$$

$$= [L]_T (\{[P]_T / [PL]\} - 1) - [P]$$

From this it follows that

$$K + [P] = [L]_T [P] / [PL]$$

Rearranging

$$[PL] = [L]_T [P] / K + [P] \quad (1)$$

### DISCUSSION

This defines a rectangular hyperbola with several important regional properties:

1. Saturation: when  $[P] \gg K$ ,  $[PL]$  asymptotically approaches  $[L]_T$ .
2. Half-saturation: when  $[P] = K$ ,  $[PL] = [L]_T / 2$  - in other word, the dissociation constant is equal to the (free) protein concentration needed to ensure that 50% of the ligand will be bounded.
3. Linearity: when  $[P] \ll K$ ,  $[PL]$  is  $\sim$  proportional to  $[P]$  with slope =  $[L]_T / K$ .

### CASE 2

Using the equilibrium relationship

$K [PL] = [L] [P]$  and substituting,

$[P]_T - [P]$  for  $[PL]$   $[L]_T - [PL]$  for  $[L]$

$[P]_T - [PL]$  for  $[P]$

Gives:

$$K \{[P]_T - [P]\} = \{[L]_T - [PL]\} \{[P]_T - [PL]\}$$

$$K [P]_T - K [P] = [L]_T [P]_T - [PL] [L]_T - [PL] [P]_T + [PL]^2$$

Rearranging

$$K [P]_T - [L]_T [P]_T + [PL] [P]_T = - [PL] [L]_T + [PL]^2 + K [P]$$

$$[P]_T \{K - [L]_T + [PL]\} = [PL] \{-[L]_T + [PL]\} + K [P]$$

Further, if we substitute

$$[L]_T = [PL] + [L]$$

Then we get

$$[P]_T \{K - [PL] - [L] + [PL]\} = [PL] \{-[PL] - [L] + [PL]\} + K [P]$$

$$[P]_T \{K - [L]\} = - [PL] [L] + K [P]$$

Which is the same as:

$$[P]_T \{K - [L]\} = K [P] - [PL] [L]$$

$$K - [L] = K \{[P] / [P]_T\} - \{[PL] / [P]_T\} [L]$$

Labeling

$[P] / [P]_T$  as  $F_{FP}$  (fraction of free protein) and  $[PL] / [P]_T$  as  $F_{BP}$  (fraction of bound protein) then above expression turn into

$$K - [L] = K F_{FP} - F_{BP} [L] \quad (2)$$

## DISCUSSION

1. If  $F_{FP} = F_{BP}=1$ , then the LHS = RHS, and the Eq. (2) is true.
2. If  $F_{FP} = F_{BP} \neq 1$ , then the LHS  $\neq$  RHS, and the Eq. (2) is invalid.

Let us now check the validity of the condition " $F_{FP} = F_{BP}=1$ ".

As per the protein conservation law,

$$[P]_T = [PL] + [P]$$

From this it follows that

$$1 = F_{BP} + F_{FP}$$

If we assume  $F_{BP} = F_{FP}=1$ , we get:

$$1 = 2$$

The condition  $F_{FP} = F_{BP} = 1$  is invalid, since 1 doesn't = 2.

In fact, the only way it can happen that  $K - [L] = K - [L]$  is if both  $F_{FP} = F_{BP}=1$ . Since  $F_{FP} = F_{BP} \neq 1$ , Eq. (2) does not therefore hold well.

## CASE NOTES

### CASE 1

If we substitute  $[L]_T - [PL]$  for  $[L]$  and  $[P]_T - [PL]$  for  $[P]$ , then equilibrium relationship  $K [PL] = [L] [P]$  becomes

$$K [PL] = ([L]_T - [PL]) ([P]_T - [PL])$$

From this it follows that

$$[PL] = [L]_T [P] / K + [P]$$

### CASE 2

If we substitute  $[L]_T - [PL]$  for  $[L]$ ,  $[P]_T - [PL]$  for  $[P]$  and  $[P]_T - [P]$  for  $[PL]$ , then equilibrium relationship  $K [PL] = [L] [P]$  becomes

$$K ([P]_T - [P]) = ([L]_T - [PL]) ([P]_T - [PL])$$

From this it follows that

$$K - [L] = K F_{FP} - F_{BP} [L] \quad (\text{wrong result})$$

## CONCLUSION

Substitution for '[PL]' along with the substitutions for '[L]' and '[P]' should be avoided in order to prevent the occurrence of wrong result.

## REFERENCES

1. Binding D B by Michael K. Gilson, [pharmacy.ucsd.edu/labs/Gilson/BindingDB-Intro.pdf](http://pharmacy.ucsd.edu/labs/Gilson/BindingDB-Intro.pdf) (2009).
2. Biochemistry by Reginald H. Garrett and Charles M. Grisham (chapter 5), © 2010 by Brooks/Cole, Cengage Learning Inc.
3. Enzymes: Biochemistry Biotechnology Clinical Chemistry by Trevor Palmer (Chapter 12), © 2001 by Horwood Pub Ltd.



**\*Corresponding Author:**

**Manjunath.R**

(Email: [manjunath5496@gmail.com](mailto:manjunath5496@gmail.com))

#16/1, 8th Main Road, Shivanagar, Rajajinagar,  
Bangalore560010, Karnataka, India